

XVIII. *New experimental researches on some of the leading doctrines of caloric; particularly on the relation between the elasticity, temperature, and latent heat of different vapours; and on thermometric admeasurement and capacity.* By Andrew Ure, M. D. Communicated by W. H. Wollaston, M. D. F. R. S.

Read April 30, 1818.

Glasgow, July 1817.

1. *On the elastic force of vapours, with new formulæ to determine it at any temperature; and a review of those given by DALTON and BIOT.*

THE phenomena attending the conversion of liquids into elastic fluids, were first accurately investigated by Dr. BLACK. He observed in the rising of vapour, and melting of ice, a beautiful system of relations, connecting and modifying the grandest operations of nature, while they were destined to afford new principles for the advancement of the arts. If it be the prerogative and characteristic of genius, to discover in the most familiar, or, as some would say, vulgar phenomena, that mystic chain of causation, which had eluded all other eyes, unquestionably, the doctrines of latent heat entitle their author to rank in the first class of philosophers.

Dr. BLACK directed his attention principally to the establishment of the general laws, which he placed on an immoveable basis; leaving to his pupils, the subordinate task of investigating their individual applications. Hence, the elastic forces of the vapours, arising from different bodies, at different temperatures, seem to have occupied him very little, if at all.

This subject was examined, however, with great ability, by two of his most distinguished friends, Professor ROBISON and Mr. WATT. The investigations of the former were published in the *Encyclopædia Britannica*, article *steam*; while we have still to regret our ignorance of those executed by the latter philosopher, with probably a more complete apparatus, and more extensive views. We are indebted to him, indeed, for some curious observation on the latent heat of steam, at different temperatures, which make us lament more, the want of those on the elastic forces themselves.

Mr. DALTON, whose peculiar speculations on caloric and meteorology led him to study the formation and variable elasticity of vapour with great attention, has since then favoured the world with many excellent dissertations, and is now reckoned the first authority on the subject. Mr. DALTON'S experiments on the steam of water were carried no higher than its ordinary boiling point; but from the observed progression of its elastic force he investigated a formula, and calculated from it a table for the higher temperatures.*

In the second number of the *Journal Polytechnique*, M. BETANCOURT, an eminent Spanish engineer, long resident at Paris, published a set of experiments on the same subject, the results of which differ from those of Mr. DALTON in many particulars, but most remarkably in the higher part of the scale.

Having had my mind often called to this important inquiry in the course of my public lectures on the applications of Science to the Arts, an apparatus of a very simple nature occurred to me, about two years ago, by which I hoped to be

* *Manchester Memoirs*, vol. v. p. 563.

able to determine, with great precision, the elastic forces of vapours at any temperature, from zero of FAHRENHEIT, to a much higher degree of heat than even BETANCOURT seems to have reached. The experiments were made soon after that time, but circumstances have till now prevented me from arranging them for publication.

With BETANCOURT's apparatus I am not acquainted, having seen only the brief table of results, inserted in our systematical works on chemistry. Professor ROBISON's consisted of a strong boiler or digester, containing the water, and furnished with three small apertures; the first receiving the bulb of a thermometer, the second covered with a safety valve, and the third having a barometer tube attached. At first I used a similar construction, but finding it hazardous, and somewhat unmanageable in the high heats, and difficult to render air tight in the lower temperatures, I abandoned it, after some unsatisfactory trials. At the low degrees of heat, the vacant part of the barometer tube introduces errors, since it has not the temperature of the boiler; and the bulb of the barometer, used in high heats, occasions a similar fallacy in the determination of the true elasticities.

Still, however, it was ingeniously conceived, and the results furnish good approximations, creditable to the celebrated experimenter.* They agree nearly with those of BETANCOURT, being obtained probably in a similar way. The method adopted by Mr. DALTON, is recommended by an elegant simplicity. It is merely a common barometer, into which a little of the vapour-giving liquid is introduced, so as to moisten, and float above the mercury. The vapour which is

* See *Encyclopædia Britannica*, vol. xvii. p. 739, 2d Edition.

generated, depresses more or less the barometric column. Hence, by subjecting the liquid to successive degrees of temperature, the corresponding depressions of the barometer, or elasticities of the vapour, are obtained.

The only difficulty in this mode of operating, is to bring a considerable length of vertical tube to an uniform temperature.

Mr. DALTON, well aware of this source of error, obviated it in a great measure, by taking a series of different tubes, decreasing in their lengths with the increasing expansions of the vapour, and concomitant descent of the mercurial column. In several experiments conducted on this plan, I found it scarcely possible to obtain results rigidly corresponding with each other, when the column of vapour, exposed in the barometer tube to the influence of surrounding heat, exceeded two inches in length.

M. BIOT, in his system of physics recently published, while he adopts Mr. DALTON's results as the basis of his reasoning, treats fully of this difficulty, and suggests an ingenious means of avoiding it. "We have had occasion several times to
" remark," says he, "that the temperature of a mass of liquid
" which cools in the air, is not entirely the same at the bottom,
" as it is at the top of the vessel; because the colder particles
" subside into the lower strata, by the excess of their weight.
" Thus the temperature of the column of hot water, which
" surrounds the tube in the preceding experiment, cannot
" be rigorously uniform throughout its whole height. We
" may endeavour to render it equal, by agitating and mingling
" the different strata of which it is composed; but this would

“ be attended with no little difficulty. It would be better to
 “ have several thermometers suspended at different heights,
 “ in the body of the water, and to take the arithmetical mean
 “ of their indications. Or otherwise, which would probably
 “ be more exact, we might employ a thermometer having a
 “ cylindrical bulb, equal in length to the column of vapour.
 “ It would then be necessary that the column of water should
 “ rise sufficiently above this vapour to allow the thermo-
 “ meter bulb to be equally immersed, or we must make on
 “ its indications the small correction mentioned p. 59, in
 “ order to reduce the temperature of the cylinder of mercury,
 “ to the temperature of the reservoir. The employment of
 “ such a thermometer may appear at first sight sufficiently
 “ difficult, since it seems that the length of the cylindrical
 “ reservoir must be very considerable, if the elastic force of
 “ the vapour be great.* ”

He then proceeds to show how this difficulty may be ob-
 viated (as indeed it had previously been by Mr. DALTON), by
 taking barometer tubes successively shortened, as the force
 of the steam is augmented by heat. He proposes to use four,
 between the freezing and boiling points of water, each being
 two decimeters, or nearly 8 inches long, and the thermometer
 bulb having also that length. The plan which I imagined, as
 it completely obviates the source of errors arising from the
 large and variable space occupied by the vapour, supersedes
 the necessity of employing M. Bior's singular remedy. It
 likewise avoids other complications, introduced by the heat-
 ing and consequent elongation of the mercurial column itself

* *Traité de Physique*. Tome I. p. 268.

attending all the other methods; and scarcely capable of being exactly appreciated at high temperatures with the apparatus of Professor ROBISON.

The space over which the vapour extends in my instrument, need never be greater than half an inch of a barometer tube, against the side of which part the oblong bulb of a delicate thermometer rests, so as to indicate the true temperature. And though the liquid and incumbent vapour are thus always restricted to the summit of the barometer tube, we can, notwithstanding, measure its progressive range of elasticity, from zero of FAHRENHEIT to one hundred, or even two hundred, degrees above the boiling point of water, from an elasticity of 0.07 of an inch, to that capable of sustaining 14 feet, or even 36 of mercury. Fig. 1 (Pl. XIX.) represents the construction employed for temperatures under and a little above the boiling point. Fig. 2 and 3 are used for higher temperatures; the last is the more convenient of the two. Each was suspended from a lofty window ceiling, and placed in a truly vertical position by means of a plumb line.

One simple principle pervades the whole train of experiments; which is, that the progressive increase of elastic force developed by heat from the liquid, incumbent on the mercury at $l' l''$, is measured by the length of column which must be added over L , the primitive level below, in order to restore the quicksilver to its primitive level above, at l . These two stations, or points of departure, are nicely defined by a ring of fine platina wire twisted firmly around the tube.

At the commencement of the experiment, after the liquid well freed from air has been let up, the quicksilver is made a tangent to the edge of the upper ring, by cautiously pouring

mercury in a slender stream into the open leg of the syphon D. The level ring below is then carefully adjusted.

From the mode of conducting my experiments, there remained always a quantity of liquid in contact with the vapour, a circumstance essential to accuracy in this research.

Suppose the temperature of the water or the oil in A to be 32° F., as denoted by a delicate thermometer, or by the liquefaction of ice; communicate heat to the cylinder A, by means of two argand flames, playing gently on its shoulder at each side. When the thermometer indicates 42° , modify the flames or remove them, so as to maintain an uniform temperature for a few minutes. A film or line of light will now be perceived between the mercury and the ring at *l*, as is seen under the vernier of a mountain barometer when it is raised a few feet off the ground. Were the tube at *l* and L of equal area, or were the relation of the areas experimentally determined, then the rise of the quicksilver above L would be one half, or a known submultiple of the total depression, equivalent to the additional elasticity of the vapour at 42° above that at 32° . Since the depressions, however, for 30 or 40 degrees in this part of the scale are exceedingly small, one half of the quantity can scarcely be ascertained with suitable precision, even after taking the above precautions. And besides, the other sources of error, or at least embarrassment, from the inequalities of the tube, and from the lengthening space occupied by the vapour, as the temperature ascends, render this method of reduction very ineligible.

By the other plan we avoid all these evils. For whatever additional elasticity we communicate to the vapour above *l*, it will be faithfully represented and measured, by the

mercurial column which we must add over *L*, in order to overcome it, and restore the quicksilver under *l* to its zero or initial level, when the platina ring becomes once more a tangent to the mercury.*

At *E* a piece of cork is fixed, between the parallel legs of the syphon, to sustain it, and to serve as a point by which the whole is steadily suspended.

For temperatures above the boiling point, the part of the syphon under *E* is evidently superfluous, merely containing in its two legs a useless weight of equipoised mercury. Accordingly for high heats, the apparatus fig. 2, or 3, is employed, and the same method of procedure is adopted. The aperture at *O*, fig. 3, admits the bulb of the thermometer, which rests as usual on *l''*. The recurved part of the tube is filled with mercury, and then a little liquid is passed through it to the sealed end. Heat is now applied by an argand flame to the bottom of *C*, which is filled with oil or water, and the temperature is kept steadily at 212° for some minutes. Then a few drops of quicksilver may require to be added to *D''* till *L''* and *l''* be in the same horizontal plane. The farther conduct of the experiment differs in no respect from what has been already described. The liquid in *C* is progressively heated, and at each stage mercury is progressively added over *L''* to restore the initial level, or volume at *l''*, by equipoising the progressive elasticity. The column above *L''* being measured, represents the succession of elastic forces. When this column is wished to extend very high, the vertical tube requires to be placed for support in the groove of a long wooden prism.

* Rings of other metals will not suit; for their expansions being much greater than that of glass, they become loose with the elevation of temperature.

The height of the column in some of my experiments being nearly 12 feet, it became necessary to employ a ladder to reach its top. I found it to be convenient in this case, after observing that the column of vapour had attained its primitive magnitude, to note down the temperature with the altitude of the column; then immediately to pour in a measured quantity of mercury nearly equal to three vertical inches, and to wait till the slow progress of the heating again brought the vapour in equilibrio with this new pressure, which at first had pushed the mercury within the platina ring at *l*". When the lower surface of the mercury was again a tangent to this ring, the temperature and altitude were both instantly observed.

This mode of conducting the process will account for the experimental temperatures being very often odd and fractional numbers. I present them to the public as they were recorded on the instant in that particular repetition of the experiment which I consider most entitled to confidence. To trim and fashion the results into an orderly looking series, would have been an easy task; but in my opinion this is a species of deception very injurious to the cause of science, and a deviation from the rigid truth of observation, which ought never to be made for any hypothesis. We shall afterwards have ample opportunities of exposing the fallacy of such premature geometrical refinements.

The thermometers were constructed by CREIGHTON, with his well known nicety, and the divisions were read off with a lens, so that $\frac{1}{10}$ of a degree could be distinguished. After bestowing the utmost pains in repeating the experiments during a period of nearly two months, I found that the only way of removing the little discrepancies, which crept in

between contiguous measures, was to adopt the astronomical plan of multiplying observations and deducing truth from the mean. It is essential to heat with extreme slowness and circumspection, the vessels, A, B, C. One repetition of the experiment occupies on an average 7 hours.

TABLE I.

The elastic force of the vapour of water in inches of mercury.

Temp.	Force.	Temp.	Force.	Temp.	Force.	Temp.	Force.	Temp.	Force.	Temp.	Force.
24°	0.170	115°	2.820	195°	21.100	242°	53.600	270	86.300	295.6	130.400
32	0.200	120	3.300	200	23.600	245	56.340	271.2	88.000	295	129.000
40	0.250	125	3.830	205	25.900	245.8	57.100	273.7	91.200	297.1	133.900
50	0.360	130	4.366	210	28.880	248.5	60.400	275	93.480	298.8	137.400
55	0.416	135	5.070	212	30.000	250	61.900	275.7	94.600	300	139.700
60	0.516	140	5.770	216.6	33.400	251.6	63.500	277.9	97.800	300.6	140.900
65	0.630	145	6.600	220	35.540	254.5	66.700	279.5	101.600	302	144.300
70	0.726	150	7.530	221.6	36.700	255	67.250	280	101.900	303.8	147.700
75	0.860	155	8.500	225	39.110	257.5	69.800	281.8	104.400	305	150.560
80	1.010	160	9.600	226.3	40.100	260	72.300	283.8	107.700	306.8	154.400
85	1.170	165	10.800	230	43.100	260.4	72.800	285.2	112.200	308	157.700
90	1.360	170	12.050	230.5	43.500	262.8	75.900	287.2	114.800	310	161.300
95	1.640	175	13.550	234.5	46.800	264.9	77.900	289	118.200	311.4	164.800
100	1.860	180	15.160	235	47.220	265	78.040	290	120.150	312	167.000
105	2.100	185	16.900	238.5	50.300	267	81.900	292.3	123.100	Another expert.	
110	2.456	190	19.000	240	51.700	269	84.900	294	126.700	312°	165.5

The apparatus employed in obtaining these results, has the peculiar advantage over all others, that the mercurial column is never heated. It is the concurrent opinion of all chemical philosophers, that caloric travels downwards in liquids with extreme slowness and difficulty. Indeed, Count RUMFORD'S experiments led him to infer that heat could not descend in fluids at all.

It is evident that in my constructions, figures 1, 2, and 3, only that small portion of quicksilver, within the vessels

A, B, and C, will be affected by the heat, but the measuring column is beyond the reach of its influence.

A surprising accordance will be perceived between my numbers, and those given by Mr. DALTON between 32° and 212° , though mine were obtained with a different modification of apparatus. Above the boiling point, where the table of Mr. DALTON is deduced from calculation, the accordance soon ceases. But as my apparatus and mode of using it were precisely the same as in the former part of the range, my results, if entitled to confidence in the one case, must be so in the other. At 280° BETANCOURT's number and mine are not much different, the former being 105 inches, the latter 102. Being perfectly convinced, by repeating the experiments in different circumstances, that Mr. DALTON's ratio of progression, though apparently accommodated to the intervals between 32° and 212° , could not serve for the higher ranges,* I endeavoured to discover a simple rule of more general application. It is above 212° , indeed, that for the purposes of art, the knowledge of the force of steam is required.

I first tried the differential method, so useful for determining the distant links of a concatenated series.

Without doing much violence to the above numbers, the forces corresponding to 100° , 110° , 120° , 130° , 140° , and 150° , may be written in a series of which the 5th order of differences = 0. Then if d' d'' d''' d^{iv} d^v , represent the first terms, in the first, second, third, fourth, and fifth order of differences, the n^{th} term of the series is

* Dr. YOUNG remarks on DALTON's ratio, "It is certain that this cannot be the law of nature, since about 394° the elasticity would become uniform, and then decrease, if the law be true." YOUNG's Natural Philosophy, 4to. vol. ii. p. 398.

$$a + \frac{1}{n-1} \cdot d', + \frac{1}{n-1} \cdot \frac{n-2}{2} \cdot d'', + \frac{1}{n-1} \cdot \frac{n-2}{2} \cdot \frac{n-3}{3} \cdot d''', + \frac{1}{n-1} \cdot \frac{n-2}{2} \cdot \frac{n-3}{3} \cdot \frac{n-4}{4} \cdot d''', + \&c,$$

In the above series for steam, $d' = 0.65$, $d'' = 0.19$, $d''' = 0.04$, $d^{iv} = 0.01$, $d^v = 0$. $a = 1.92$.

Example 1st. To determine the 8th term in the series, or the elastic force at 8×10 , above 90° , (the first term 100° being included) or at 170° .

Here $n = 8$

$$\begin{array}{r} a + \frac{1}{n-1} \cdot d' = 1.92 + 4.55 = 6.47 \\ \frac{1}{n-1} \cdot \frac{n-2}{2} \cdot d'' = 4.08 \\ \frac{1}{n-1} \cdot \frac{n-2}{2} \cdot \frac{n-3}{3} \cdot d''' = 1.40 \\ \frac{1}{n-1} \cdot \frac{n-2}{2} \cdot \frac{n-3}{3} \cdot \frac{n-4}{4} \cdot d^{iv} = 0.35 \\ \hline 12.30 \end{array}$$

Observation gives 12.05, forming a good accordance.

Example 2. Required the 10th term, or $n = 10$. For 190° F.

$$\begin{array}{r} a + \frac{1}{n-1} \cdot d' = 7.77 \\ \frac{1}{n-1} \cdot \frac{n-2}{2} \cdot d'' = 6.84 \\ n-1 \cdot \frac{n-2}{2} \cdot \frac{n-3}{3} \cdot d''' = 3.36 \\ n-1 \cdot \frac{n-2}{2} \cdot \frac{n-3}{3} \cdot \frac{n-4}{4} \cdot d^{iv} = 1.26 \\ \hline 19.23 \end{array}$$

At 190° experiment makes it 19.00, still coinciding nearly.

By the same equation we find the 20th term or for 290° to be 124.28, while experiment gives 120.15, showing a difference of 4.13 inches. At a higher point the error becomes greater. We here see that a geometrical series may coincide

apparently through a considerable range with experiment, and yet be inaccurate when farther extended.

Dissatisfied, therefore, with this approximation, I prosecuted the inquiry, and had the happiness to discover a very simple and beautiful ratio, which will actually apply through an extensive scale of temperature, and is incomparably easier in practice than the preceding rule. The elastic force at $212^{\circ} = 30$ inches being divided by 1.23, will give the force for 10° below; this quotient divided by 1.24, will give that for 10° lower; and so on progressively. To obtain the forces above 212° , we have merely to multiply 30 by the ratio, 1.23 for the force at 222° ; this product by 1.22 for that at 232° , and thus for each successive interval of 10° above the boiling point.

Thus $30 \times 1.23 = F_{222^{\circ}}$. $30 \times 1.23 \times 1.22 = F_{232^{\circ}}$,
using F to denote the force at any temperature n , according to the notation of LAPLACE.

By departing from the point of 210° F., we shall obtain results equally accurate, but more convenient for comparison with the experimental table. The following numbers exhibit the correspondence of this ratio with actual observation.

TABLE II.

Observed elasticity of aqueous vapour compared with the ratios.

Temp.	Calcul. Force.	Expert.	Temp.	Calcul. Force.	Expert.	DALTON.	BETANC.	ROBISON.
210°	28.9	28.9	210°	28.9	28.9	28.84	28.8	28.65
200	23.5	23.6	220	35.54	35.54	34.99		35.80
190	19.0	19.0	230	43.36	43.10	41.75	45.5	44.70
180	15.2	15.16	240	52.46	51.70	49.67		54.90
170	12.07	12.05	250	62.95	61.90	58.21		66.80
160	9.50	9.60	260	74.91	72.30	67.73	80.17	80.30
150	7.42	7.58	270	88.39	86.30	77.85		94.10
140	5.75	5.77	280	103.41	101.90	88.75	105.12	105.90
130	4.42	4.36	290	119.95	120.15	100.12		
120	3.37	3.33	300	137.94	139.70	111.81		
110	2.55	2.45	310	157.25	161.30	123.53		
100	1.92	1.86	320	177.70		135.00		
90	1.43	1.36						
80	1.06	1.01				Temp.	BETANC.	ROBISON.
70	0.77	0.726						
60	0.56	0.516				32°	0.0	0.0
50	0.40	0.36				50		0.12
40	0.28	0.25				80	0.81	0.82
30	0.20	0.19				100	1.65	1.60
20	0.14	0.14				120	2.95	3.00
10	0.098					140	5.00	5.15
0	0.068					160	9.00	8.65
						180	14.00	14.05
						200	22.50	22.62

The rule on which the preceding table is formed, may be expressed in a manner better fitted to give *directly* the elastic force corresponding to any given temperature moderately distant from 212°. It becomes also more accurate.

Let r = the mean ratio between 210° and the given temperature; n = the number of terms (each of 10°) distant from 210°; F = the elastic force of steam in inches of mercury.

Then, $\text{Log. of } F = \text{Log. } 28.9 \pm n. \text{Log. } r$; the positive sign being used above, the negative below 210°.

Or by common arithmetic, multiply or divide 28.9, according as the temperature is above or below 210°, by the mean ratio, involved to a power denoted by the number of terms. The product or quotient is the tension required.

Example 1st. The temperature is 140°. What is the corresponding elasticity of the vapour from water heated to that point?

140° is 7 terms of 10° each *under* 210°; 1.26 is the mean ratio = $\frac{1.23 + 1.29}{2}$; and, consequently, $r = 1.26$; $n = 7$.

	Log. 28.9 =	1.46090
Log. 1.26 × 7 =	0.10037 × 7 =	<u>− 0.70259</u>
		0.75831, which is
the logarithm of	-	5.732 inches.
Experiment gives	-	5.77, difference .04, inconsiderable.

Example 2. What is the tension of steam at the temperature of 290°?

$r = \frac{1.23 + 1.16}{2} = 1.195$	$n = 8$
Log. 28.9	= 1.46090
8. Log. $r = 8 \times 0.07737$	= + <u>0.61896</u>
Log. of 140.02 inches	2.07986

At 290° by experiment = 120.15

Example 3. Temperature 250°. Force of steam in contact with water?

$r = \frac{1.23 + 1.20}{2} = 1.215$	$n = 4$
Log. 28.9	= 1.46090
4 Log. $r = 4 \times 0.08458$	= + <u>0.33832</u>
Log. of 62.98	1.79922

At 250° Experiment 61.90

At these high heats, it is very possible that the experiment may be in error by 1 inch, which is the whole difference here. About half a degree of FAHRENHEIT misnoted, would give this deviation.

Such a correspondence, therefore, of observation with the calculated results, shows that we have found a rule of perfect accuracy for all purposes of engineering, &c. If I am asked whether this formula coincides at every link with the chain of nature, I freely acknowledge, that I do not imagine it strictly so to do. But still it affords approximations such, that within moderate limits, I cannot tell whether to place more confidence in them, or in those found by experiment. It has moreover the rare advantage of being extremely simple, and level to the capacity of all practical men.

In Bior's excellent work above quoted, where many of the hitherto vague disquisitions of physical science have been happily brought within the pale of geometry, this celebrated philosopher has deduced, from Mr. DALTON's experiments on the force of steam, a general formula for determining its elasticity at any temperature.

In investigating this formula, he represents the decrease of the logarithms of the elastic forces by a series of terms of the form $an + bn^2 + cn^3$; abc being constant coefficients.

$$\text{Thus, } \text{Log. } F_n = \text{Log. } 30 + an + bn^2 + cn^3$$

It is unnecessary to employ powers of n higher than the cube, because their coefficients would be insensible, as the calculation will show. To determine the coefficients abc , he makes use of the elastic forces, observed at the temperatures on the centigrade scale of 100° , 75° , 50° , and 25° ; whence result these conditions,

$n = 0$	$F = 30.00$ inches
$n = 25$	$F_{25} = 11.25$
$n = 50$	$F_{50} = 3.50$
$n = 75$	$F_{75} = 0.910$

Substituting these conditions in the above general formula, and bearing in mind that the logarithm of a fraction is equal to the logarithm of the numerator minus the logarithm of the denominator, we have the three following equations of conditions.

$$\begin{aligned} -0.4259687 &= 25. a + 625 b + 15625 c. \\ -0.9330519 &= 50. a + 2500 b + 125000 c. \\ -1.5180799 &= 75. a + 5625 b + 421875 c. \end{aligned}$$

Doubling the first, and subtracting it from the second, a disappears; trebling it, and subtracting it from the third, a also disappears. Then dividing each of the resulting equations by the coefficient of b , we have

$$\begin{aligned} -0.00006489160 &= b + 75 c. \\ -0.00006404635 &= b + 100 c. \end{aligned}$$

Subtracting the one of these from the other, b will disappear; and dividing it by the coefficient of c , we shall have c . Next, by substituting the value of c in one of these equations, we get b . Lastly, putting b and c in one of the two first equations, we have a . Thus we find

$$\begin{aligned} a &= -0.01537419550 \\ b &= -0.00006742735 \\ c &= +0.00000003381 \end{aligned}$$

Whence the whole formula $\text{Log. } F_n = \text{Log. } 30 + an + bn^2 + cn^3$ is completely determined, and may serve for calculating F_n , relative to any proposed value of n .

If we make, for example, $n = 100$, we shall have the elastic force at 100 degrees below the boiling point, or at the temperature of melting ice. We thus obtain

$$\text{Log. } F_n = 1.4771213 - 2.1778831 = - 0.7007618.$$

Or employing negative indices in order to make use of the ordinary logarithmic tables,

$$\text{Log. } F_n = \bar{1}. 2992382, \text{ whence}$$

$$F_n = 0. 19917 \text{ inches; and observation gives us } 0. 200.$$

The error is obviously insensible; and we may adopt, says M. BIOT, our formula as representing the experiments of Mr. DALTON. To introduce the FAHRENHEIT degrees into the formula, calling them f , and counting from 212° , we have $\frac{5}{9}f = n$; and substituting this value of n in the preceding formula, we obtain

$$a = - 0. 00854121972$$

$$b = - 0. 00002081091$$

$$c = + 0. 00000000580,$$

whence $\text{Log. } F_f = 1.4771213 + af + bf^2 + cf^3$, f being the number of degrees of FAHRENHEIT, reckoning them from 212° , positive below and negative above this point of departure.

By the above formula, thus elaborately investigated by M. BIOT, I have computed the elastic forces of steam at the three successive temperatures of 232° , 262° and 312° , or 20° , 50° and 100° , above the boiling point of FAHRENHEIT'S scale.

In the first case we have $f = - 20$ and $af + bf^2 + cf^3 = 20 + 400b - 8000c$; f is negative, being above the point of departure 212° , and, consequently, the products af and cf^3 are positive, while bf^2 becomes negative.

$$\begin{aligned} 20 a &= 0.170824 \\ 400 b &= - 0.008324 \\ 8000 c &= + 0.000046 \end{aligned}$$

$$0.162546 + \log. 30 \text{ or } 1.477121$$

$$1.477121$$

$$\text{Log. of } 43.62 = 1.639667$$

By BIOT's formula therefore at 232 F.	-	43.620
My experiments	-	44.700
Mr. DALTON's table	-	43.25
BETANCOURT	-	47.20

By M. PUILLET's table at the end of BIOT's 1st vol.

computed from the above formula - 43.500

The difference between BIOT and my experiments here is only 1.10 inches.

2d Example. Temperature 262° FAHR. $f = 50$

$$\begin{aligned} 50 a &= 0.4270609 \\ 2500 b &= - 0.0520272 \\ 125000 c &= + 0.0007250 \end{aligned}$$

$$0.3757587$$

$$\text{Log. } 30 = 1.4771213$$

$$\text{Log. of } F_{262^\circ} = 1.8528800 \quad F_{262^\circ} = 71.265$$

Experiment 74.600

DALTON's table 69.700

PUILLET's table 70.800

BETANCOURT 82.500

The disparity between BIOT's formula and experiment becomes more apparent now: it amounts to 3.335 inches.

At 266° FAHR. which corresponds to 130° centigrade, I make it from BIOT'S first formula 77.053, while at 130° by M. POUILLET, it is 75.68;* difference 1.973. Finally,

At the temperature of 312°, $f = 100$

$$\begin{array}{r} 100 a = 0.854121972 \\ 10.000 b = - 0.208109100 \\ 1000000 c = + 0.005800000 \\ \hline 0.651812872 \\ 1.477121300 \\ \hline \end{array}$$

$$\text{Log. of } F_f = 2.128934172 \quad F_f = F_{100} = 134.57$$

Experiment gives 167.00

Mr. DALTON'S table 125.85

The difference between experiment, and both calculations, is now excessive, and even between the two latter it amounts to nearly 9 inches.

From this ample investigation, we may legitimately conclude, that we ought to receive such geometrical representations with great caution. M. BIOT, indeed, with a candour becoming his genius, admits these formulæ to be merely tentative approximations. The high reputation of this philosopher, and the geometrical skill here displayed, might have led the scientific world to repose confidence in his formula, within the limits of $55\frac{1}{2}$ degrees centigrade = 100 FAHR. It was therefore entitled to a deliberate examination.

It is curious to observe that my very simple formula, $\text{Log. } F = \text{Log. } 28.9 \pm n. \text{ Log. } r$, gives good approximations,

* 130° centigr. gives by M. P. force of vapour = 1907.07 millimetres, of which taking 25.4 to the English inch, we have $\frac{1907.07}{25.4} = 75.08$ as above.

through a much more extensive range, than the elaborate formula of the distinguished French geometer. Even when carried so high as the 310th degree of FAHR., we have

$$\text{Log. } 28.9 + n. \log. r = 2.19810 = L, F_{100}; \text{ hence}$$

$$F_{100} = 157.8$$

Experiment gives 161.3, a difference of only $3\frac{1}{2}$ inches at this prodigious elasticity; which may be deemed altogether unimportant in practice.

BIOT's formula gives a result 31 inches, and Mr. DALTON's 40 in defect.

Of Professor ROBISON's higher numbers, it is merely necessary to examine the successive differences for every 10° above 212° . These are 7.2, 8.9, 10.2, 11.9, 13.5, 13.8, 11.8, and the second differences are $+ 1.7 + 1.3 + 1.7 + 1.6 + 0.3 - 2.0$.

Such striking irregularities cannot exist in the progression of nature. BETANCOURT's are liable to a similar censure. We may find indeed small discrepancies in the best observations at such temperatures.

§ II. *Experiments to determine the elastic forces of the vapours of alcohol, ether, oil of turpentine, and petroleum or naphtha.*

The determination of the elasticities of these vapours is a very interesting problem in chemical philosophy. It may possibly unfold the law which connects temperature and elastic energy, and it may furnish likewise some useful applications.

Mr. DALTON has examined the subject with considerable care.

My experiments were performed with the apparatus above described, and were verified by frequent repetitions. The following results were noted down during the progress of the experiments.

TABLE III.

Elastic forces of the vapours of alcohol, ether, oil of turpentine, and petroleum or naphtha.

Ether.		Alcohol sp. gr. 0.813.		Alcohol sp. gr. 0.813.		Petroleum.	
Temp.	Force of Vapour.	Temp.	Force of Vapour.	Temp.	Force of Vapour.	Temp.	Force of Vapour.
34°	6.20	32	0.40	193°·3	46.60	316°	30.00
44	8.10	40	0.56	196.3	50.10	320	31.70
54	10.30	45	0.70	200	53.00	325	34.00
64	13.00	50	0.86	206	60.10	330	36.40
74	16.10	55	1.00	210	65.00	335	38.90
84	20.00	60	1.23	214	69.30	340	41.60
94	24.70	65	1.49	216	72.20	345	44.10
104	30.00	70	1.76	220	78.50	350	46.86
		75	2.10	225	87.50	355	50.20
2nd.	Ether.	80	2.45	230	94.10	360	53.30
		85	2.93	232	97.10	365	56.90
105°	30.00	90	3.40	236	103.60	370	60.70
110	32.54	95	3.90	238	106.90	372	61.90
115	35.90	100	4.50	240	111.24	375	64.00
120	39.47	105	5.20	244	118.20	Oil of Turpen.	
125	43.24	110	6.00	247	122.10	Temp.	Force of Vapour.
130	47.14	115	7.10	248	126.10		
135	51.90	120	8.10	249.7	131.40	304°	30.00
140	56.90	125	9.25	250	132.30	307.6	32.60
145	62.10	130	10.60	252	138.60	310	33.50
150	67.60	135	12.15	254.3	143.70	315	35.20
155	73.60	140	13.90	258.6	151.60	320	37.06
160	80.30	145	15.95	260	155.20	322	37.80
165	86.40	150	18.00	262	161.40	326	40.20
170	92.80	155	20.30	264	166.10	330	42.10
175	99.10	160	22.60			336	45.00
180	108.30	165	25.40			340	47.30
185	116.10	170	28.30			343	49.40
190	124.80	173	30.00			347	51.70
195	133.70	178.3	33.50			350	53.80
200	142.80	180	34.73			354	56.60
205	151.30	182.3	36.40			357	58.70
210	166.00	185.3	39.90			360	60.80
		190	43.20			362	62.40

Remarks on the preceding table.

The ether of the shops as prepared by the eminent London apothecaries, boils generally at 112° ; but when washed with water, or re-distilled, it boils at 104° or 105° . It may by rectification, however, be made to boil at a still lower temperature.

Concerning the boiling point of oil of turpentine, curious (may we say ridiculous) discrepancies exist in our systems of chemistry. Dr. MURRAY, for example, in the table of the scale of temperature at the end of the first volume of his valuable system, last edition, places the boiling point of oil of turpentine at 560° . Mr. DALTON, vol. 1. p. 39. of his new system of chemical philosophy, says "several authors have it that oil of turpentine boils at 560° . I do not know how the mistake originated, but it boils below 212° , like the rest of the essential oils." I made with much care several experiments on this point, previous to ascertaining the force of its vapour, and found its boiling point to be about 316° . When recently distilled, however, it will boil at 305° . Did it boil below, or even at 212° , as Mr. DALTON asserts, *then*, long before the included portion in the above experiments had reached the 304^{th} degree, it would have acquired such an elasticity as to support a high column of mercury, instead of being barely *in equilibrio* with the atmospheric pressure.

Plunge a phial half filled with fresh oil of turpentine into a metal cup containing any fixed oil. Heat the cup gradually. It will be found that, at the temperature of 316° , the oil remains in steady ebullition, as indicated by a thermometer suspended in the centre of the phial. Prior to this, even at

212°, some small bubbles will be evolved, principally owing to the moisture dispersed in the pores of the oil, from the water originally mixed with the crude turpentine in its distillation. If the heat be very rapidly thrown in, while the upper surface of the oil of turpentine has the area only of a one or two ounce phial, it is possible to heat it to 360° or 370°, in apparent contradiction to the theory of latent heat; for when a liquid boils in an open vessel, according to Dr. BLACK, its temperature should remain stationary. The true cause of this phenomenon is developed towards the conclusion of this memoir. The specific caloric of the vapour of the volatile oil is so small, compared to that of water, that the heat may readily be quicker introduced than the boiling process can abstract it. Concerning the boiling point of this oil, I have since inquired of a manufacturer; and he states its boiling point at 320°. Essential oil of rosemary, when kept for some time, boils at 270°; recent oil at 212°. To assign the cause of this difference, is foreign to our present object.

The vapour of ether follows nearly the same rate of expansion as water, if we start from their respective boiling points. This was observed also in Mr. DALTON's experiments; and from this single analogy, chiefly, he laid down the general law, "that the variation in the force of vapour from all liquids
" is the same for the same variation of temperature, reckon-
" ing from vapour of any given force."

My experiments on oil of turpentine and petroleum show the fallacy of this generalization, if we reckon the common thermometric scale a tolerably correct index of temperature; but if, with Mr. DALTON, we consider our thermometric scale,

as very erroneous, then ether itself is an exception to its own law, to use this paradoxical, though just expression. In consequence of his peculiar thermometric ideas, Mr. DALTON has abrogated the above law, which he had himself framed; though it is curious to observe, in some respectable treatises on chemistry, both hypotheses detailed, without indicating their mutual incompatibility. M. BIOT, likewise, far from imagining that the law had been repealed for 8 or 9 years, proposes to judge by its provisions of the total elastic force of every vapour at 100° centigrade, to serve as the basis of the determination of their respective specific gravities at that temperature.*

My experiments show that from 105° to 167°.5 FAHRENHEIT, ether trebles the tension of its vapour, as water also does from 212° to 272°.7; both containing nearly, but by no means exactly, equal intervals of the FAHRENHEIT graduation. According to Mr. DALTON's corrected scale of temperature, we have,

$$\begin{array}{rcl} 212^\circ \text{ FAH.} & = & 212^\circ \text{ DALTON.} \quad 105^\circ \text{ FAH.} = 119^\circ \text{ DALTON.} \\ 273 \text{ F.} & = & 256.4 \text{ D.} \quad 167.5 \text{ F.} = 176 \text{ D.} \end{array}$$

real interval = $\frac{256.4 - 119}{212 - 105} = 44.4$ by DALTON. By DALTON $\frac{176 - 119}{167.5 - 105} = 57$ = the real interval of temperature.

Thus we see, that while the interval for trebling the tension of ethereal vapour is 57°, that for aqueous vapour is only 44°.4; quantities that are to each other nearly as 100: 80. Hence, according to this eminent chemist, ether must take for

* "On peut calculer par la loi de M. DALTON, quelle doit être, pour chacun d'eux, la force élastique totale de sa vapeur à la température de 100 degrés." *Traité de Physique*, Tome i. p. 393.

trebling the force of its vapour a fifth part more heat than water does.

I hope presently to be able to adduce satisfactory experimental evidence, that our thermometric indications are not at all so unequable as Mr. DALTON conceives.

Meanwhile, in examining closely the table of the vapour of ether, a beautiful analogy with that of water presented itself. The series of ratios representing the progression of the latter being lowered a single step, will accurately fit the former. At 30 inches of elasticity 1.23 was our initial number for aqueous vapour; for ethereal, it becomes 1.22; increasing or diminishing by unity each time in the second decimal figure, according as we descend or ascend by intervals of 10° of the FAHRENHEIT scale.

The following is a general view of the results.

TABLE IV.

The observed tension of ethereal vapour compared with the ratios 1.22, 1.23, &c. and 1.22, 1.21, &c.

Temp.	Quotients.	Expert.	Temp.	Product.	Expert.
104°	—	30.00	105°	—	30.0
94	24.7	24.70	115	36.6	35.9
84	20.2	20.00	125	44.3	43.24
74	16.3	16.10	135	53.4	51.9
64	13.06	13.00	145	63.6	62.1
54	10.3	10.3	155	75.4	73.6
44	8.1	8.1	165	88.2	86.4
34	6.35	6.2	175	102.0	99.1
			185	117.3	116.1
			195	134.0	133.7
			205	151.3	151.3

The numbers derived from calculation give a surprising accordance with those observed in the lower range. In the

upper range, the correspondence is as good as the delicacy of the experiments at such temperatures could permit us to expect. The experiments have been presented without modification. I must own, that when first the above perfect coincidence appeared, it gave me no small pleasure, as it led me to suppose that I had discovered the hidden chain of nature.

In treating of the vapour of alcohol, Mr. DALTON considers it as irregular in the progress of its elastic force by heat, owing to its not being a homogeneous liquid. He suspects "that the elastic force in this case is a mixture of aqueous and alcoholic vapour." I cannot see the cogency of this argument; for, if the separate bodies have a regular progression, the mixture ought not surely to be anomalous. I believe, however, that if the experiments were made with due accuracy, alcohol would be found as methodical in the elastic march of its vapour as other bodies. The following table will afford satisfactory proofs of the justness of these views. For absolute alcohol, the progression is probably as simple as that of the preceding vapours. But for alcohol, sp. gr. 0.813, which though highly rectified, contains not a little water, we should expect it to result from a composition or modification of ratios. After some search on this principle, I accordingly found it. Starting from the boiling point 174° , or for the convenience of comparison with the table, from the decade 170° , we move not by a unit, as before, but by a unit and a tenth; or the initial ratio 1.26 is affected at each step or term of 10° , with the number ± 0.011 , the signs being employed as in the preceding cases.

TABLE V.

Elastic force of the vapour of alcohol compared with the ratios.

Temp.	Calculat.	Observed.	Temp.	Calculat.	Observed.	Temp.	Calculat.	Observed.
250°	130.24	132.3	170°	28.3	28.3	90°	3.41	3.4
240	111.13	111.24	160	22.46	22.6	80	2.52	2.45
230	93.94	94.1	150	17.7	18.0	70	1.85	1.76
220	78.67	78.5	140	13.8	13.9	60	1.35	1.23
210	65.29	65.0	130	10.65	10.6	50	0.97	0.86
200	53.69	53.0	120	8.16	8.10	40	0.69	0.56
190	43.76	43.2	110	6.2	6.00	30	0.49	0.38
180	35.35	34.73	100	4.67	4.50			

$$\frac{28.3}{1.26} = 22.46 \therefore 28.3 \times \frac{1.26 - .011}{1.26 - .011} = 35.35$$

$$28.3 \times \frac{1.26 - .011}{1.26 - .022} = 43.76 \text{ \&c.}$$

$$\frac{22.46}{1.271} = 17.7, \text{ \&c.}$$

The correspondence here exhibited between the observed and calculated elasticities is remarkable; nor does the difference ever exceed what would be produced by an error of 1° in the construction or reading off of the thermometer. This may fairly be deemed the limit of accuracy in such an experiment.

Oil of turpentine is regulated by the constant ratio 1.122, which converts any elastic force into that 10° above or below, multiplying as usual in the former, and dividing in the latter case. For petroleum the ratio is 1.14; it is also constant.

The following table exhibits a comparative view of theory and experiment.

TABLE VI.

Oil of Turpentine.			Petroleum.		
Temp.	Calculat.	Observed.	Temp.	Calculat.	Observed.
310°		33.5	320°		31.7
320	37.7	37.06	330	36.2	36.4
330	42.5	42.1	340	41.2	41.6
340	47.7	47.3	350	47.0	46.86
350	53.5	53.8	360	53.6	53.3
360	60.4	60.8	370	61.1	60.7

The whole of the preceding research is closely interwoven with a question of the first importance in chemical philosophy; what are the relative portions of temperature denoted by the graduations of our thermometric scale? Mr. DALTON regards the progressive elasticities of aqueous and ethereal vapour as affording countenance, if not support, to his thermometric innovations. He affirms, that if our instrument for measuring heat were accommodated to his doctrine, the quantity of expansion of its mercury is as the square of the temperature from its freezing point; then “the force of steam in contact with water increases *accurately* in geometrical progression to equal increments of temperature, provided these increments are measured by a thermometer of water or mercury, the scales of which are divided by the above mentioned law.”*

Were this position true, it would certainly bring a powerful analogy in aid of his theoretical views. We are now furnished with *data* to verify, or refute it. The following tables show the correspondence between that principle and experiment. In the table of aqueous vapour, the *first* column pre-

* New System, vol. i. p. 11.

sents his geometrical progression of that vapour, co-ordinate with his equal intervals of real temperature contained in the *second*. In the *third*, are the corresponding points of the common scale, as given by Mr. DALTON. To these points the elastic forces, as determined by experiment, are placed opposite in the fourth column.

Table second, for vapour of ether, is similarly arranged; the first three columns being Mr. DALTON's; the *fourth*, the faithful transcript of observation.

“ The force of the vapour of sulphuric ether,” says Mr. DALTON, “ in contact with liquid ether, is a geometrical progression, having a less ratio than that of water.” “ Ether, as manufactured in the large way, appears to be a very homogeneous liquid. I have purchased it in London, Edinburgh, Glasgow, and Manchester, at different times, of precisely the same quality in respect to its vapour.”* This shows that no exception can be made to my experiments on account of a supposed difference in the quality of the ether. From the mode of conducting my experiments, there remained always a quantity of liquid ether in contact with the vapour, a circumstance essential to accuracy in this research. The results were verified by frequent repetitions, and discover, in my opinion, the consistency of truth.

* New System, vol. i, pp, 20, 21.

TABLES VII. AND VIII.

DALTON'S theory of the thermometric scale, compared with the observed temperatures and tensions of vapours.

Aqueous Vapour.				Ethereal Vapour.			
DALTON'S geom. progression of elasticity.	DALTON'S new scale of temperat.	FAHREN.	Observed elasticity.	DALTON'S progression of elasticity.	DALTON'S scale.	FAHREN.	Observed elasticity.
22.7 inch.	202°	199°	23.1 in.	6.1	32°	32°	5.81
30.0	212	212	30.0	9.16	52	46.6	8.67
39.5	222	225	39.11	13.77	72	62.55	12.60
52.0	232	238.6	50.3	20.65	92	79.84	18.40
69.0	242	252.6	64.5	31.0	112	98.50	27.2
91.0	252	266.8	81.5	46.54	132	118.50	37.7
120.0	262	281.2	103.5	69.88	152	139.9	56.8
158.	272	296.2	131.7	104.91	172	162.4	83.3
208.	282	311.5	164.8	157.5	192	186.5	118.3
				236.5	212	212	169.0

The numbers of the first and fourth column ought evidently to agree, if the theory be just. Their differences, on the contrary, are prodigiously great. At 272° of his scale, for example, equal to 296°.2 of ours, the law of progression makes the elastic force of aqueous vapour amount to 158 inches : experiment gives 131.7 ; and I am confident, that the latter cannot be in error above an inch or two. Again at 262°, equivalent to 281°.2 FAHRENHEIT, his theory gives the force of the same vapour at 120 inches ; by observation it is only 103.5. Now at this part of the scale, my result is confirmed by the concurrence of those obtained by BETANCOURT and ROBISON. I consider this demonstration complete. If we compare these very elasticities of Mr. DALTON, with the table formerly given by the same philosopher,* we shall find

* Manchester Memoirs, vol. 5.

discordances which no ingenuity can harmonize. At that time, 225° of FAHR. = 222° of the new scale, gave a force of vapour equal to 38.3; it is now $39.5.252^{\circ}.6$ F. = 242° D. then coincided with an elasticity of 58.6 inches; above, it is 69. And finally, $281^{\circ}.2$ F. = 262° D. were opposite to 90 inches; they have become here 120. And yet no new experiments on the vapour of water have been adduced, to justify such immense alterations.

It may be said, indeed, that these changes arise merely from the substitution of one hypothesis for another; but the deviations from experiment are even more remarkable, since as 282° new scale, correspond to $311^{\circ}.5$ FAHR., the difference amounts to 43 inches, being more than one fourth of the total elastic force generated at that high temperature.

When we turn our attention to ether, we find the discrepancies, if possible, less easy to reconcile. At the temperature of 212° , for example, where the old and new scales meet for the last time, the force of its vapour by the geometrical progression exceeds that found from experiment, by the enormous quantity of 67 inches and a half; amounting to two fifths of the whole elastic force evolved.

May we venture, then, to conclude, from these multiplied comparisons, that the progressions of elasticity in vapours, taught by Mr. DALTON, are geometrical fictions, intended to quadrature with his notions concerning temperature; but not consonant with the laws or phenomena of nature?

Within a moderate compass, indeed, it is not difficult to suit the ratio of elastic force and the thermometric graduation to each other; but the prosecution of the enquiry into ranges more remote, detects the fallacy of such hypothetical adapta-

tions. My experiments on the vapours of water, alcohol and ether, seem to show, that the ratio of tension decreases in a certain progression as the temperature augments. Were the ratios 1.23, 1.22, 1.21, &c., which are seen to apply so well to aqueous vapour for a considerable range above 212° , to be adopted as representing the progressive march of nature, it would lead to the absurd conclusion, that at 240° above the boiling point, or 452° F., the farther influx of caloric would occasion a diminution of elasticity in the steam. The truth however is, that at the 312th degree, indications of a divergence begin to appear between the two lines of experiment and calculation, which had run for so long a space nearly parallel. The curve representing the expansive force of steam, I consider to be logarithmic, in which the ratios, as ordinates, continually diminish, without ever vanishing, or coming to an equality. The axis is an asymptote to the curve, as in the atmospherical logarithmic.

CHAPTER II.

On thermometric admeasurement, and the doctrine of capacity.

Before inquiring into the relative quantities of heat, contained in different vapours at the same tension, it will be proper to determine the primary and fundamental proposition concerning the measure of temperature. It is singular, that not one experimental fact has been advanced, capable of settling this question, amid the contending opinions of chemical philosophers. Mr. DALTON has, in particular, exerted all the resources of his genius and science to destroy our confidence in the thermometric scale; our sole guide in the vast

and intricate province of caloric. While I hope to be able to fix this now indeterminate point, by a new train of investigations, and consequently to prove the entire fallacy of his doctrine of temperature, the key-stone of his system of heat, I do not mean to affirm the absolute uniformity of expansion in bodies, by equal increments of that power. I think it indeed highly probable, that every species of matter, both solid and liquid, follows an increasing rate in its enlargement by caloric. Each portion that enters into a body must weaken the antagonist force, cohesion; and must therefore render more efficacious the operation of the next portion that is introduced. Let 1000 represent the cohesive attraction at the commencement; then, after receiving one increment of caloric, it will become $1000 - 1 = 999$. Since the next unit of that divellent agent will have to combat only this diminished cohesive force, it will produce an effect greater than the first, in the proportion of 1000 to 999; and so on in continued progression. That the increasing ratio is, however, greatly less than Mr. DALTON maintains, may, I think, be clearly demonstrated.

According to his table of equal increments of temperature, vol. i. p. 14, New System, we have the following intervals, corresponding to the five successive intervals of 90° on our scale.

From 32° to 122° , to 212° , to 302° , to 392° , to 482° .

Intervals by FAHR. of 90° , 90° , 90° , 90° , 90° .

True intervals by DALTON, $102^\circ.4$ $77^\circ.6$ $63^\circ.9$ $55^\circ.7$ $50^\circ.5$

The relative inequality of these intervals is deduced from Mr. DALTON's law, that "all pure homogeneous liquids, as water and mercury, expand from the point of their congela-

“tion, or greatest density, a quantity always as the square of the temperature from that point.” He regards the law as resulting from the constitution of liquids, and therefore not applicable to solid bodies. This is indeed implied in its enunciation. In p. 43, after assigning reasons, he states, “that for all practical purposes we may adopt the notion of “the equable expansion of solids.”

Now I am prepared to prove, either, that the expansion of solids partakes of the above inequability of liquids, which nobody imagines, and for which no reason, even hypothetical, can be assigned; or, which is the only alternative, that homogeneous solids, and mercury, proceed almost exactly, *pari passu*, in their rates of expansion by heat.

The experiments which justify this assertion were made by me about five years ago, and were then exhibited to many of my chemical friends, as also in my public lectures; but a wish to render the series more complete, has induced me to withhold them from the public eye, till requisite leisure could be afforded for this purpose. They were performed with a pyrometer of peculiar construction, in an oblong trough filled with melting ice: a strong bar of Swedish iron was placed, from which projected at right angles, four inflexible iron arms, attachable by powerful screws to any part of the bar. The arms nearest the extremities of the bar, carried each a fine micrometer microscope, made by that admirable artist Mr. TROUGHTON. The other two arms were incurvated downwards at their extremities, which supported a metallic or other rod. This was fixed by two pinching screws at one end, but lay loose on a friction roller at the other. The loose end bore an elevated index. The curvature of these two arms was

such as to allow their extremities, with the attached rod, to be plunged *beneath the surface of oil or water, about an inch*, contained in a copper trough. This was placed parallel to the large trough, and a few inches distant from it.

The copper vessel was slowly and equably heated, by a series of argand lamps placed beneath. One micrometer watched a point projecting from the arm that held the fixed extremity of the rod. The oil was carefully agitated during the application of the heat; and the bulbs of three thermometers, mutually comparable, were immersed into it at regular distances. The micrometers were screened from the influence of the heat. They rendered the $\frac{1}{20000}$ of an inch discernible, and even a smaller quantity, by an experienced eye.

A rod of pure Swedish iron, or of such pure copper as jewellers use for alloying gold, being adjusted to the apparatus, the point on the micrometer scale, that appeared a tangent to the small luminous aperture in the thin index plate of steel, was noted down, when the liquid in the trough was at 32° . The value and truth of the micrometrical indications had been previously ascertained, by viewing through the microscopes a given surface or aperture, moved laterally, so as to make its image successively coincide with the different points of the interior notched scale.

Heat being now applied, the progressive march of the index across the field of view of the micrometer microscope was closely observed, and its position written down at intervals of 10° or 20° of the FAHR. thermometer. But as the pyrometrical details will appear in a separate memoir on the expansions of bodies, I shall state here merely what concerns the present subject.

If we denominate the absolute elongation of the heated metallic rod from 32° to 122° , 10, then its elongation from 122° to 212° ; from 212° to 302° ; from 302° to 392° ; from 392° to 482° , was in each successive interval of 90° F, as nearly as possible 10 also. The slight irregularities, incident to all delicate experimental investigations, being often in opposite directions, in different repetitions of the same experiment; or those which manifested themselves in the ascending or elongating range, were neutralized, so to speak, by others of an inverse nature, which appeared in the cooling retrocession. Here, the movements of the liquid mercury and of the solid rod by heat proceeded, *pari passu*, through a very great extent of temperature. Let us now recollect that these 5 increments, which on our thermometer are equivalent to $5 \times 90^{\circ} = 450^{\circ}$; and which altogether produce five times the elongation that the first interval occasions, constitute, on Mr. DALTON's scale, only 350° . If we call the first interval given by this philosopher 1.00, then the four succeeding intervals contain a range of temperature on his scheme, of only two and a half times the first; and therefore only two and a half times additional elongation should have been produced, instead of four times, as found by experiment. "Since for all practical purposes uniform increments of bulk, or expansions of *solids* by heat, correspond to uniform increments of this power;" then each of our old successive intervals of 90° may, for all practical purposes, be held to correspond to equal increments of temperature.

Mr. DALTON's intervals from 32° to 482° FAHR. are as before given, $102^{\circ}.4$; $77^{\circ}.6$; $63^{\circ}.9$; $55^{\circ}.7$; $50^{\circ}.5 = 350^{\circ}.1$. Now, if we call the first quantity 1.00, it will produce on a

metallic rod a corresponding effect in expansion = 1.00. The next interval of Mr. DALTON's scale (equal always to 90° FAHR.) can produce only $\frac{3}{4}$ of the effect of the first, or as 75 to 100. The third, fourth, and fifth intervals will give the fractional expansions in reference to the first, of $\frac{6^2}{100}$, $\frac{5^4}{100}$, and about $\frac{5^0}{100}$, or merely a half.

No such diminution of effect was observed in the experiments; from 392° to 482° F., the rod elongated as much as from 32° to 122°, or double the quantity compatible with the DALTONIAN hypothesis. Thus therefore we have a rigid, and I think unanswerable demonstration of the general correctness of the common scale of temperature, and of the extreme inaccuracy and inapplicability of Mr. DALTON's geometrical substitute. Should the preceding statement leave any doubt or obscurity concerning the legitimacy of the inference now drawn, I trust it will be entirely removed, when the details of the experiments are published, with drawings of the apparatus, in my treatise on pyrometry.

Yet though the mercury in the thermometer tube move, *pari passu*, with a metallic rod, deemed uniform in its expansion, it does not prove perfectly equal uniformity of expansion to belong to the mercury. It will seem, no doubt, a paradoxical assertion, that of two bodies marching together, hand in hand, one of them may have an equable pace, while that of the other is regularly, but very slowly accelerated. Yet I think the position just. It proceeds from a circumstance in the thermometer sufficiently obvious, but which seems to have escaped our *systematic* writers. I do not rest the proposition on any imperfection of workmanship, or supposed irregularity in the expansions of the glass

Let us take a thermometer, the calibre of whose stem is perfectly uniform, and whose scale is exactly divided. Let it have a range from zero to the 656th degree, at which mercury boils, by the accurate experiments of CREIGHTON. At 32°, let the mercury stand at the bottom of the ivory scale, where of course the graduations commence. The bare part of the instrument is consequently the plunging limit, in most chemical researches on the temperature of liquids. Immerse the bulb in common oil, or oil of vitriol heated to 212°; $\frac{1}{3}$ * part of the whole included mercury, will now ascend above that part of the stem plunged in the liquid. The part actually exposed to the heat, and by whose expansion the column on the scale is supported, is only $\frac{2}{3}$ of the initial mass. Augment the heat of the oil till the instrument indicate 392°; we know that there remains now, under the immediate influence of the heat, $\frac{1}{3}$ nearly of the original weight of mercury; and finally, at 572°, only about $\frac{2}{3}$ rest in the immersed part of the stem and bulb.

$\frac{2}{3}$ or $\frac{1}{3}$ parts may be considered as no longer subjected to the power of caloric. If the thermometer stem were recurved near the bulb, the mercury in the stem placed horizontally would be cold; and this proposition would be almost exactly true.

Now, since the calibre and divisions are uniform, the capacity of the tube from the point marked 212°, to that marked 392°; and again from this, to that opposite to 572°, is in each equal to its capacity from 32° to 212°. Hence these three equal capacities are filled by the expansions of the three unequal quantities of mercury 62, 61, 60. At the

* A minute fraction less; but we need not complicate the statement with it.

highest station, the column of quicksilver equal on the stem to $3 \times 180^\circ$, is sustained by the expansion of 60 parts; at the middle point, $2 \times 180^\circ$ is supported by that of 61; and at 212° there are 62 parts of mercury to sustain 180° in the tube. Or, to put it in another form, these three successive spaces on the scale are equal; the first portion of mercury is protruded into it by the expansion of 62 parts in the bulb; the second portion by the expansion of 61; and the third by that of 60.

Therefore, if these three thermometric intervals of 180° , each of which holds an equal measure of mercury, contain also equal increments of temperature, as denoted by the equal increments of a metallic rod; then, these three equal effects are produced from the unequal quantities of mercury 62, 61, 60. This liquid, then, must have an increasing rate of expansion, the inverse of these numbers, for every 180° of the scale, or $\frac{1}{62}$, $\frac{1}{61}$, $\frac{1}{60}$. That is to say, 60 parts at 572° do the same work by the same power of caloric, as 61 at 392° , and 62 at 212° .

I believe this to be the real nature of mercurial expansion, and the true condition of the thermometer; which is an equable measurer of heat, because the mercury possesses the above increasing rate of expansion. Were the mercury, on the contrary, absolutely uniform in its augmentations of volume by equal increments of heat, then for an instrument whose bulb alone in practice can be immersed, the three above ranges should have the corresponding parts of the scale shortened in the successive proportions of 62 to 63; 61 to 63; and 60 to 63; quantities taken together nearly equal to 9° , or $= 3 \times \frac{3}{82} \times 180 = \frac{810}{82}$.

Whatever reception these speculations may experience, they must not be confounded with the experiments on the expansions of metallic rods, and the corollaries, which have a distinct and independent existence.

§ II. *On the doctrines of capacity, as connected with the preceding investigation.*

Dr. CRAWFORD and DE LUC, tried to verify the justness of the thermometric indications, by mixing together water at 212° and 32° ; when the former found 122° , and the latter 119° , to be the resulting temperature. DE LUC's number is 3° below the mean; Dr. CRAWFORD's is exact. This ingenious philosopher afterwards sought to confirm the evidence thus given to the accuracy of the scale, by other experiments, which were however of rather an equivocal import. Both of the above results have been condemned and rejected by Mr. DALTON: he states the true mean temperature to be not 122° , nor even 119° , but 110° . For this deviation, the reasons which he assigns appear, independently of all arguments derived from other quarters, to be in themselves inconclusive. He says, "the temperature of the above mixture ought to be found above the mean 122° ." "Water of these two temperatures (32° and 212°) being mixed, loses about $\frac{1}{90}$ of its bulk. This condensation of its volume* must expel a quantity of heat, and raise the temperature above the mean." p. 7. Again, p. 50, "that water *increases* in its capacity for heat with the increase of temperature, I consider demonstrable from the following arguments. 1st. A

* That condensation of volume in a liquid, is no proof of the expulsion of heat, is shown in my Essay on Sulphuric Acid.

“ measure of water at any one temperature mixed with a
“ measure at any other temperature, the mixture is less than
“ two measures. Now, a condensation of volume is a certain
“ mark of diminution of capacity and increase of temperature,*
“ as in the mixture of sulphuric acid and water ; or the effects
“ of mechanical pressure, as with elastic fluids. Second,
“ when the same body suddenly changes its capacity by a
“ change of form, it is always from a less to a greater as the
“ temperature ascends ; for instance, ice, water and vapour.
“ Third, Dr. CRAWFORD acknowledges from his own ex-
“ perience, that dilute sulphuric acid, and most other liquids
“ he tried, he found to increase in their capacity for heat with
“ the increase of temperature. Admitting the force of these
“ arguments, it follows, that when water of 32° and 212° are
“ mixed, and give a temperature denoted by 119° of the
“ common thermometer, we must conclude that the true mean
“ temperature is somewhere below that degree. I have
“ already assigned the reason why I place the mean at 110° .”
Now the only reason I can elsewhere find, is derived from his
general law, “ that all homogeneous liquids expand, as the
square of the temperature, from the point of greatest density
or congelation.” In p. 7, he ventures to assert nothing more
than, “ that it is not improbable that the true mean tempe-
“ rature between 32° and 212° , may be as low as 110° FAH-
“ RENHEIT.”

Satisfied from my pyrometrical experiments, that his
general hypothesis of the expansion of liquids being as the

* For the entire fallacy of this reasoning, see my Essay just quoted ; expansion of
volume should by Mr. D. increase capacity and diminish temperature. The very
reverse is shown in that paper.

square of their temperature, is totally inapplicable to mercury, the inference relative to the thermometric mean between 32° and 212° cannot be allowed. But let us examine, on their own merits, the preceding arguments against Dr. CRAWFORD and DE LUC's verification of the mean temperature between that of freezing and boiling water.

The reasoning derives its sole force from the assumption, that the capacity of water for heat, increases as its temperature is raised. There is adduced, however, no fact in the least decisive on this main point. What analogy is there between the entire change of form and constitution suffered by an incompressible liquid, on becoming an elastic vapour, and the progressive heating of the liquid itself? Or, although dilute sulphuric acid and other liquids should increase in their specific caloric on being heated, which however has not been satisfactorily demonstrated, are we to assert that water must do so too? It is a matter of surprize to me, that a philosopher of Mr. DALTON's judgement and acuteness should have pressed such inconclusive analogies into his service. He knew well that water is endowed with some curious peculiarities, when compared with other liquids, or anomalies, as we idly stile them; for they constitute no anomaly in nature, but wisely fit water for performing the important functions assigned to it in the economy of our globe.

In a series of experiments, carefully conducted on the relative capacities for heat, of water, sulphuric acid, oil of turpentine, and spermaceti oil, published in my Essay on hydrochloric acid and the chlorides; it seems to be directly demonstrated that the specific heat of water does not *increase*, but actually *diminishes*, and that very conspicuously, as its

temperature rises. It is there proved, that from 210° to 150° FAHR. the specific heat of oil is to that of water as 597 to 1000; and from 150° to 90° as 513 to 1000. The same proportional difference of relation is exhibited by the other two liquids. Now, were the phenomenon occasioned by the oil of vitriol, common oil, and oil of turpentine, increasing in *their* capacities for heat in a still more rapid ratio than water, we should undoubtedly expect, from the innate differences between the specific heats of these three substances, to find that they would move independently on each other, or at different rates. But *their* uniform advance together, while water alone varies in this respect, shows distinctly, that in the water resides the cause of the variation. This reasoning may be illustrated in many ways, but by nothing more clearly than the exploded astronomical system of the diurnal and annual movements of the sun and fixed stars; in support of which, very extravagant hypotheses had to be contrived.

The single fact of the motion of the earth once admitted, reduced the PTOLEMAIC chaos to order. If, in like manner, we should suppose an increasing ratio in the specific heat of water, then we must also suppose a much more rapid increase in the ratios of the above three substances, although their individual specific heats are greatly inferior to that of water. Ought not that body, which has of all others the most decided relation to heat, or highest specific heat, to have also its ratio most decidedly or rapidly augmented? In adopting the increasing specific heat of water, we must farther assume, that, however different the initial specific heats of the above three liquids may be, yet, while they possess all the same rate of increase, water alone has a different one; an inadmissible supposition. All

these difficulties and contradictions are removed at once by the experimental fact, that water is endowed with a decreasing ratio in its capacity for caloric, as its temperature is augmented.

Since finishing the above researches on specific heat, I have been led to examine attentively the systematic accounts of this subject in our chemical treatises; and I find that BERTHOLLET, with a sagacity peculiar to himself, had anticipated, from the chemical constitution of bodies, such an experimental result as I have recently obtained; though the statements then prevalent all militated against his views. “If caloric
“obey the usual laws of attraction, when it is in small
“quantity, relative to the body to which it is united, it will
“enter into more intimate combination; and hence the elas-
“ticity or expansive energy of it, on which temperature
“depends, may be overcome, and a larger quantity be required
“to produce a given temperature. Hence, the quantity of
“caloric contained in bodies in the first stage of temperature,
“may be greater than it will be higher in the scale.”

In the Essay above referred to, I have shown that this circumstance in water, renders it peculiarly qualified for serving as the magazine and equalizer of the temperature of the globe. Since at our ordinary atmospherical heats, it possesses the greatest capacity for caloric, small variations in its temperature give it a great modifying power over the circumambient air. Although the doctrine of final causes be no safe guide to the discovery of unknown truths, yet when it concurs with experiment, we may deem it an agreeable confirmation. This is finely illustrated by Count RUMFORD'S speculations on the maximum density of water being placed

several degrees above its point of congelation ; a fact which does not hold with regard to any other homogeneous liquid.

If the specific heat of water, then, diminish as its temperature advances from the freezing to the boiling point, an interval of 10° near 32° , will contain more caloric than ten degrees near 122° , and still more than the same intervals near 212° . On this principle we can readily account for the results obtained by Mr. DALTON, in mixing with water at different temperatures a known proportion of ice ; though it is remarkable that this able chemist did not see in them any thing inconsistent with his own opposite views upon specific heat.

“ $176^{\circ}.5$ expresses the number of degrees of temperature, “ such as are found between 200° and 212° of the old or com- “ mon scale, entering into ice of 32° , to convert it into water of 32° ; 150° of the same scale suffice, he says, for the same effect, between 122° and 130° : and between 45° and 50° , 128° are “ adequate to the conversion of the same ice into water. “ These three resulting numbers (128 , 150 , 176.5) are nearly “ as 5 , 6 , 7 . Hence it follows, that as much heat is necessary “ to raise water 5° in the lower part of the old scale, as is “ required to raise it 7° in the higher, and 6° in the middle.”*

Mr. DALTON, instead of adopting the obvious conclusion, that the capacity of water for heat is greater at lower than it is at higher temperatures, and that therefore a smaller number of degrees of the former should melt as much ice as a greater number of the latter, ascribes the deviation denoted by these numbers, or their differences, to the gross errors of our thermometric graduation ; which he considers

* *New System*, vol. i. p. 53.

so excessive, as not only to equal, but greatly to overbalance the real increase in the specific heat of water ; which left to its own operation, would have produced opposite experimental results.

That our thermometric scale has no such prodigious deviation from truth, or uniformity of indication, I conceive to be fully established, and therefore the only legitimate inference from these very experiments of Mr. DALTON, is the *decreasing* capacity of water with the increase of its temperature.

It deserves to be remarked, that my experiments on the relative times of cooling a globe of glass, successively filled with water, oil of vitriol, common oil, &c. give exactly the same results as Mr. DALTON derived from mixtures of 2 ounces of ice and 60 of water. This concurrence is the more satisfactory, since, when the Essay on hydrochloric acid was written, I had no recollection of Mr. DALTON's experiments. I found that from 210° to 150° the specific heat of oil bears to that of water the ratio of 597 to 1000 ; and from 150° to 90° , that of 513 to 1000. Now, at his highest and middle temperatures of 200° and 120° , which come nearest to mine of 180° and 120° , we have by him the ratio of 176.5 to 150° .

But $597 : 513 :: 176 : 150$ exactly, which is a very striking coincidence, and affords the happiest confirmation of the accuracy of both sets of experiments, as well as of the justness of the principles on which they were conducted, and on which, particularly, my reductions were founded. We now see the reason why, when equal weights of water at 32° and 212° are mixed, the temperature may be *below* the mean, as was found by DE LUC. The capacity at the middle tempe-

perature, is greater than the mean capacity of the two extremes, (that is of the ingredients mixed, ice, cold and boiling water) and therefore the thermometric tension will be lessened, and its mercury will descend on the scale.* This diminution of temperature will cause a corresponding diminution of bulk, which affords a complete answer to Mr. DALTON's first and only plausible argument, formerly quoted against Dr. CRAWFORD's deductions, and the opinions of DE LUC. With regard, however, to these experiments, of mixing hot and cold water to find a mean temperature, there are sufficient difficulties to render the result uncertain to 2 or 3 degrees. Hence, nothing of moment can safely be inferred from them.

Concerning sulphuric acid in its various states of dilution, I beg to refer the reader to my Essay on the subject, where he will find several peculiarities relative to its volume at different acid strengths, that entirely change its relations to caloric. I have not seen these formerly adverted to by any chemist. They were evidently unknown to Mr. DALTON.

CHAPTER III.

On the latent heat of different vapours.

What relation is there between the caloric existing in the vapours of different substances, and the temperatures at which they respectively acquire the same elastic force?

On this subject I am not acquainted with any preceding inquiries, though a question of such interest has probably not escaped examination.

* Taking Mr. DALTON's three numbers as correct: then $\frac{176.5 + 128}{2} = 152^{\circ}.25$. But 150° in the middle are equal to the former mean of the two. Hence, the proposition in the text is demonstrated.

In this research I employed a very simple apparatus; and with proper management, I believe it capable of giving the absolute quantities of latent heat in different vapours, as exactly as more refined and complicated mechanisms. At any rate, it will afford comparative results with great precision.

It consisted of a glass retort of very small dimensions, with a short neck inserted into a globular receiver of very thin glass, and about three inches in diameter. The globe was surrounded with a certain quantity of water at a known temperature, contained in a glass basin. 200 grains of the liquid, whose vapour was to be examined, were introduced into the retort, and rapidly distilled into the globe by the heat of an argand lamp. The temperature of the air was 45° , that of the water in the basin from 42° to 43° , and the rise of temperature, occasioned by the condensation of the vapour, never exceeded that of the atmosphere by 4 degrees. By these means, as the communication of heat is very slow between bodies which differ little in temperature, I found, that the air could exercise no perceptible influence on the water in the basin during the experiment, which was always completed in 5 or 6 minutes. A thermometer of great delicacy was continually moved through the water; and its indications were read off, by the aid of a lens, to small fractions of a degree.

In all the early experiments of Dr. BLACK on the latent heat of common steam, the neglect of the above precautions introduced material errors into the estimate. Hence that distinguished philosopher found the latent heat of steam to be no more than 800° or 810° . Mr. WATT afterwards deter-

mined it more nearly from 900° to 950° ; and LAVOISIER and LA PLACE have made it 1000° .

It is evident that whenever the water, into which the latent heat is evolved by condensation of the vapour, becomes much hotter than the surrounding air, it will be impossible to ascertain how much of the caloric is dissipated; and consequently, the true quantity contained in the vapour must remain uncertain.

The sources of error in operating with the calorimeter of LAVOISIER and LA PLACE, were first pointed out by Mr. WEDGWOOD, and have been since commented on by Dr. THOMSON, and other good systematists. It is said to be difficult to obtain precisely uniform quantities of liquified ice in the repetition of the same experiments, with that celebrated apparatus.

From the smallness of the retort in my mode of proceeding, the shortness of the neck, and its thorough insertion into the globe, we prevent condensation by the air *in transitu*; while the surface of the globe and the mass of water being great, relative to the quantity of vapour employed, the heat is entirely transferred to the refrigeratory, where it is allowed to remain, without apparent diminution, for a few minutes. In numerous repetitions of the same experiment, the accordances were excellent. The following table contains the mean results. The water in the basin weighed in each case 32340 gr. The globe was held steadily in the centre of the water by a slender ring fixed round its neck. The distillation was rapidly performed, so that all the condensation took place in the globe.

Table of experimental results on the latent heat of different vapours.

200 gr. of water distilled, raised	32340 gr.		
water from	-	-	42°.5 to 49°
200 gr. alcohol, spec. gravity 0.825		-	42 to 45
200 gr. sulphuric ether; boiling point 112°			42 to 44
200 gr. oil of turpentine		-	42 to 43.5
200 gr. petroleum		-	42.5 to 44
200 gr. nitric acid. spec. grav. 1.494. boiling			
point 165°		-	42 to 45.5
200 gr. liquid ammonia. sp. gr. 0.978		-	42 to 47.5
200 gr. vinegar.	sp. gr. 1.007	-	42.5 to 48.5

Calculation from the above table of the specific or latent heats of the vapours.

1st, Water. $\frac{32340}{200} = 161.7 =$ the number of grains of water contained in the refrigeratory to one of steam. This proportion is constant for all the vapours.

From 42°.5 to 212° there are 169°.5; one half of which = 84°.75, or in round numbers 84°, is the rise of temperature which would be produced by adding to water at 42°.5 its own weight of boiling water; and $\frac{84}{161.7} = 0.52$, is the elevation which 200 gr. would occasion on 32340 grains.

The water was however in reality heated $6\frac{1}{2}$ degrees, or from 42°.5 to 49°. The difference, $6°.5 - 0°.52 = 5°.98$, shows the quantity of heat added to each of the 161.7 parts beyond what the same weight of boiling water would have communicated.

And $5.98 \times 161.7 = 967^\circ$, being the latent heat of the steam of water.

2d. Alcohol. Boiling point 175° . Specific gravity 0.825.

$\frac{175 - 42 \times 66.5}{2 \times 161.7} = 0.41$. 0.41 multiplied into the specific heat of liquid alcohol 0.65, is $0^\circ.266$, which represents the elevation of temperature produced by adding 200 gr. of boiling hot alcohol to 32340 gr. of water. The thermometer in the experiment rose 3° . $3^\circ - 0^\circ.266 = 2.734$, $2.734 \times 161.7 = 442^\circ$ = the latent heat of alcoholic vapour in equilibrio with the atmospheric pressure. By a similar process of calculation the latent heat of the other vapours was determined.

General table of latent heat of vapours.

Vapour of water at its boiling point			967°
alcohol	-	-	442
ether	-	-	302.379
petroleum	-	-	177.87
oil of turpentine		-	177.87
nitric acid		-	531.99
liquid ammonia		-	837.28
vinegar		-	875.00

From the phenomena exhibited in the mechanical condensation and rarefaction of gases and vapours, as well as from their general constitution, it may be inferred, that an intimate and necessary connection subsists between their latent heat, elastic force, and specific weight or density.

Hence, when their tension is the same, it appears reasonable to suppose that the product of their densities into their quantities of latent heat will also be the same. Repulsive energy

will be proportional to the quantity of heat, the repulsive power condensed or contained in a given space. Thus if the *space* left for its interposition or lodgment be in one vapour a half or a third of the amount of the space in another, we ought to find equal tension produced in the former case, by a half or a third of the latent heat required for the latter.

As the principle, I have reason to suppose, is somewhat new, let us illustrate it by an application to the three vapours in the above list which are most homogeneous, or at any rate best understood; those of alcohol, ether, and water.

Aqueous vapour of an elastic force balancing the atmospheric pressure has a specific gravity, compared to air, by the accurate experiments of GAY LUSSAC, of 10 to 16.

For facility of comparison let us call the steam of water unity, or 1.00; then the specific gravity of the vapour of pure ether is 4.00, while the specific gravity of the vapour of absolute alcohol is 2.60.

But the vapour of ether, whose boiling point is not 100°, but 112°, like the above ether, contains some alcohol; hence, we must accordingly diminish a little the specific gravity of its vapour.

It will then become instead of 4.00	-	-	3.55
Alcohol of 0.825 sp. gr. contains much water;			
specific gravity of its vapour	-	-	2.30
That of water as before, unity	-	-	1.00

The interstitial spaces in these three vapours will therefore be inversely as these numbers, or

$$\frac{1}{355} \text{ for ether; } \frac{1}{230} \text{ for alcohol; } \frac{1}{100} \text{ for water.}$$

Hence $\frac{1}{355}$ of latent heat, existing in ethereal vapour, will occupy a proportional space, be equally condensed or possess the same tension with $\frac{1}{230}$ in alcoholic, and $\frac{1}{100}$ in aqueous vapour.

A small modification will no doubt be introduced by the difference of the thermometric tensions, or sensible heats, under the same elastic force. Common steam, for example, may be considered as deriving its total elastic energy from the latent heat multiplied into the specific gravity + the thermometric tension.

Hence the elastic force of water, or

$$E_w = 970^\circ \times 1.00 + 212^\circ = 1182$$

$$E_e = 302^\circ \times 3.55 + 112^\circ = 1184$$

$$E_{al} = 440^\circ \times 2.30 + 175^\circ = 1185$$

Three equations which yield, according to my general proposition, equal quantities; or of which the differences are inconsiderable, and undeserving of notice.

Neither the specific heats nor specific gravities of the other vapours are ascertained with sufficient precision to enable us to subject them to calculation.

General equation $F - \overline{L \times D} + T = 0$: L, latent heat, D, density, T, temperature corresponding to F.

When the elastic forces of vapours are doubled, or when they sustain a double pressure, their interstices are proportionally diminished. We may consider them now as in the condition of vapours possessed of greater specific gravities. Hence, the second portion of heat introduced to give double the

elastic force need not be equal to the first, in order to produce the double tension. This view now given accords with the experiments of Mr. WATT, alluded to in the beginning of this memoir. He found that "the latent heat of steam is less when it is produced under a greater pressure or in a more dense state; and greater when it is produced under a less pressure or in a less dense state."*

BERTHOLLET thinks this fact so unaccountable, that he has been willing to discard it altogether. Whether the view which I have just opened, of the relation subsisting between the elastic force, density, and latent heat of different vapours, harmonize with chemical phenomena in general, I leave to others to determine. It certainly agrees with that *unaccountable* fact. Whatever be the fate of the investigation of the general law now respectfully offered, the statement of Mr. WATT may be implicitly received under the sanction of his acknowledged sagacity and candour.

CONCLUSION.

To the theory of latent heat, which, like the hydrostatic paradox of Archimedes, might have remained for ages a barren, though beautiful proposition, the fertile genius of that philosopher gave all at once its noblest application, and most beneficial influence on human life, by his new steam engine. After him, many minds of the first order for science and ingenuity have offered schemes of farther improvement;

* Philos. Trans. vol. 84. p. 335.

but all either frivolous or abortive; with such prophetic judgment had Mr. WATT anticipated the happiest form and structure of which it was susceptible.

Under this conviction, it is with much deference that I draw the following practical inferences from the last train of experiments.

Since the vapour of alcohol, having the same elastic force as the atmosphere, contains $\frac{44}{100}$ of the latent heat of ordinary steam, and since its elastic force is doubled at the 206th degree (6° below the boiling heat of water), with perhaps $\frac{1}{3}$ of additional caloric; might we not, in particular circumstances, employ this vapour for impelling the piston of a steam engine? The condensing apparatus could, I imagine, be so constructed, as to prevent any material loss of the liquid, while more than a quadruple power would be obtained from the same size of cylinder at 212° , with an expenditure of fuel not amounting to one half of what aqueous vapour consumes; or the power and fuel would be as 3 to 1, calling their relation in ordinary steam 1 to 1. A considerable engine could thus also be brought within a very moderate compass. Possibly, after a few operations of the air pump, the incondensable gas may be so effectually withdrawn, that we might be permitted to detach this mechanism, which, though essential to common engines, takes away one fourth of their power. In a distillery in this country, or on a sugar estate in the colonies, a trial of this plan might perhaps be made with advantage. While exercising its mechanical functions of grinding, mashing or squeezing the canes, it would be converting ordinary into strong spirit for rectification, or for

the convenience of carriage. Might not such an engine be executed on a small scale, for many purposes of domestic drudgery? It would unquestionably furnish a beautiful illustration in philosophy, to make one small portion of liquid, by the agency of fire, imitate the ceaseless circulation and restless activity of life.

Fig. 1.

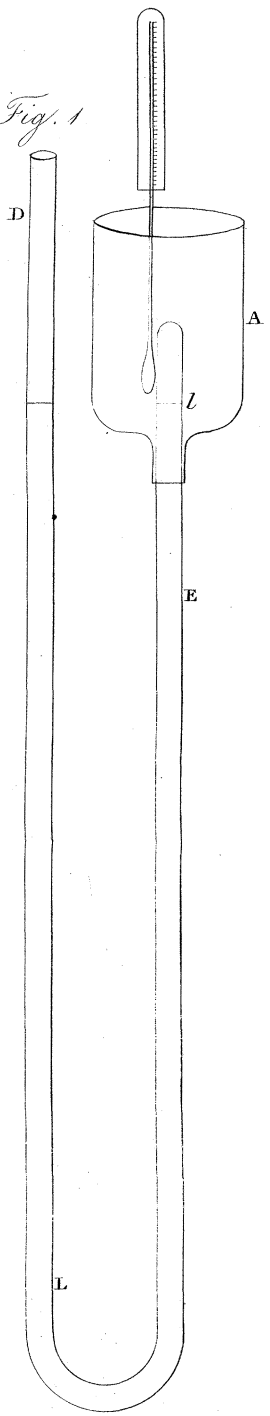


Fig. 2.

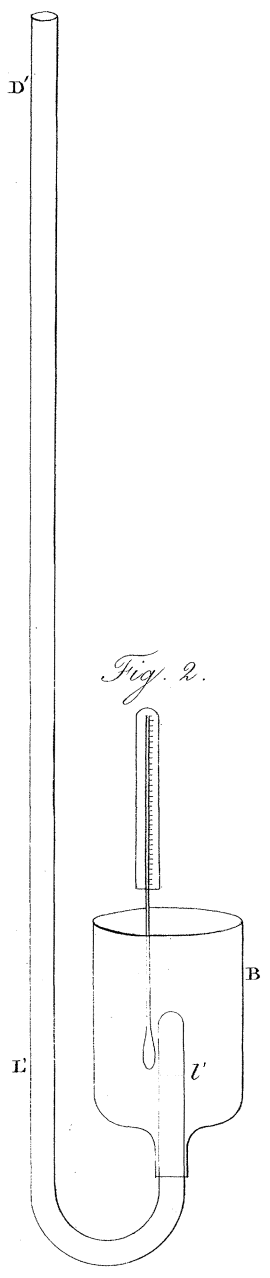


Fig. 3.

